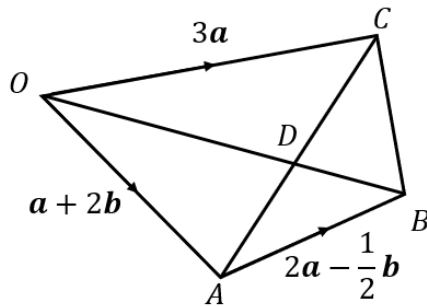


Vector Proof – Equating Coefficients

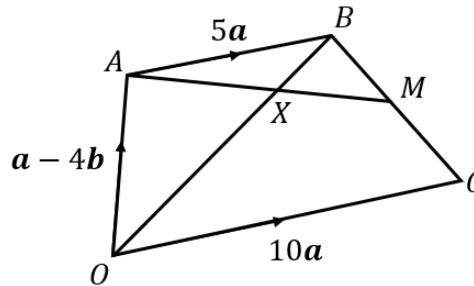
(a)

$OABC$ is a quadrilateral, where $\overrightarrow{OC} = 3\mathbf{a}$, $\overrightarrow{OA} = \mathbf{a} + 2\mathbf{b}$ and $\overrightarrow{AB} = 2\mathbf{a} - \frac{1}{2}\mathbf{b}$. The point D is on OB and AC such that $OD : OB = \lambda : 1$ and $AD : AC = \mu : 1$. By finding two ways to express the vector \overrightarrow{OD} , find the values of λ and μ .



(b)

$OABC$ is a trapezium, where $\overrightarrow{OC} = 10\mathbf{a}$, $\overrightarrow{OA} = \mathbf{a} - 4\mathbf{b}$ and $\overrightarrow{AB} = 5\mathbf{a}$. M is the midpoint of the line BC . The point X is on OB and AM such that $OX : OB = \lambda : 1$ and $AX : AM = \mu : 1$. Find the values of λ and μ and the vector \overrightarrow{OX} in terms of \mathbf{a} and \mathbf{b} .



(c)

In the triangle OAB , $\overrightarrow{OB} = 5\mathbf{b}$ and $\overrightarrow{OM} = 2\mathbf{a} + 2\mathbf{b}$, where M is the midpoint of OB . OC is the line OB produced and $\overrightarrow{OB} = \overrightarrow{BC}$. The point X is on the line AB such that $AX : AB = \lambda : 1$. Given that MXC is a straight line, find the value of λ and the vector \overrightarrow{MX} in terms of \mathbf{a} and \mathbf{b} .

