

Algebraic Proof with Multiples

(a)	(b)	(c)
<p>Show that $4(x + 3) + x - 2$ is always a multiple of 5</p> $ \begin{aligned} &4x + 12 + x - 2 \\ &= 5x + 10 \\ &= 5(x + 2) \end{aligned} $	<p>Show that $3(7 + 2x) - 9$ is always a multiple of 6</p> $ \begin{aligned} &21 + 6x - 9 \\ &= 12 + 6x \\ &= 6(2 + x) \end{aligned} $	<p>Show that $4(x + 7) + 2(1 - x)$ is always a multiple of 2</p> $ \begin{aligned} &4x + 28 + 2 - 2x \\ &= 2x + 30 \\ &= 2(x + 15) \end{aligned} $
(d)	(e)	(f)
<p>Show that $7(2x - 1) - 5(x - 2)$ is always a multiple of 3</p> $ \begin{aligned} &14x - 7 - 5x + 10 \\ &= 9x + 3 \\ &= 3(3x + 1) \end{aligned} $	<p>Show that $(x + 7)(x - 2) - x^2 - 1$ is always a multiple of 5</p> $ \begin{aligned} &x^2 + 7x - 2x - 14 - x^2 - 1 \\ &= 5x - 15 \\ &= 5(x - 3) \end{aligned} $	<p>Show that $(x + 8)(x + 1) - x(x + 5)$ is always a multiple of 4</p> $ \begin{aligned} &x^2 + 8x + x + 8 - x^2 - 5x \\ &= 4x + 8 \\ &= 4(x + 2) \end{aligned} $
(g)	(h)	(i)
<p>Show that $(x + 5)^2 + (x - 3)^2$ is always a multiple of 2</p> $ \begin{aligned} &x^2 + 10x + 25 + x^2 - 6x + 9 \\ &= 2x^2 + 4x + 34 \\ &= 2(x^2 + 2x + 17) \end{aligned} $	<p>Show that $(3x + 5)(2x - 1) + (2x - 1)(x + 3)$ is always a multiple of 4</p> $ \begin{aligned} &6x^2 + 7x - 5 + (2x^2 + 5x - 3) \\ &= 8x^2 + 12x - 8 \\ &= 4(2x^2 + 3x - 2) \end{aligned} $	<p>Show that $(3x + 2)^2 - (x + 4)(3x - 2) + 4(x - 3)$ is always a multiple of 6</p> $ \begin{aligned} &9x^2 + 12x + 4 - 3x^2 - 10x + 8 + 4x - 12 \\ &= 6x^2 + 6x \\ &= 6(x^2 + x) \end{aligned} $